Errata et corrigenda

ANALYTIC COMBINATORICS

by P. Flajolet and R. Sedgewick

(Cambridge University Press, ISBN-13: 9780521898065)

Relative to the edition of January 2009, of which a free electronic version is available at http://algo.inria.fr/flajolet/books/ June 6, 2010

> Cuiusvis hominis est errare, nullius nisi insipientis in errore perseverare. — MARCUS TULLIUS CICERO (Oratio Philippica Duodecima).

Thanks to all those who send corrections or detect typos! This will prove highly valuable in preparing the next edition/printing.

P. 1, last display. Eliminate the spurious ",," before the period in the equation giving "31!".	Manuel Kauers 16/09/2009
P. 10, figure caption. "Right: a binary" becomes "Right: A binary". (Unify capitalization in such figure captions.)	Manuel Kauers 16/09/2009
P. 16, line 9. Read as "Part B of this book, <i>Complex Asymptotics</i> ." (I.e., insert comma).	Manuel Kauers 16/09/2009
P. 18, footnote. Read: "a reference such <u>as</u> ".	
P. 25, line 2. Get rid of overfull hbox at the end of the line.	Manuel Kauers 16/09/2009
P. 31, last paragraph, "kown" becomes "known".	Ayla Gafni 24/07/2009
P. 35, two lines after Eq. (30): "great depth" replaces "geat depth"	Christopher Hanusa 12/08/2009
P. 39, 3rd line of the table in Figure I.6. "5244589437" becomes "5244589437". (I.e., insert "" in source file to separate the 10 digits into two blocks of five digits each.)	Manuel Kauers 16/09/2009
P. 42, line -5. Change "of daisy-artichoke-rabbit fame In particular" to "of daisy-artichoke-rabbit fame. In particular". (I.e., insert period.)	Manuel Kauers 16/09/2009
P. 62, line -6. Read as "over an $r$ letter alphabet".	Manuel Kauers 16/09/2009

l Kauers 2009	P. 66, line -15. Overfull hbox at the end of the line.
l Kauers 2009	P. 66, line -2. It is perhaps clearer to read as "the c
l Kauers 2009	P. 67, line -9. Insert a long space (\qquad) after the
ppher Hanusa 2009	P. 77, Eq. (80). The figure could be cleaned.
Chapman 2009	P. 81, three lines below Equation (85). The equation " $\mathcal{H} = \mathcal{Z} + \mathcal{Z} \times \mathcal{H} + \mathcal{Z} \times \mathcal{H} \times \mathcal{H}$ ".
	P. 86, Note I.60; line +2, read as "view $\mathcal{A}$ "; second d change italics to calligraphic.]
opher Hanusa 2009	P. 89, proof of Theorem I.5, last displayed equation. d and the vertical bar in " $d \mid n$ ".
l Kauers 2009	P. 95, footnote. "Schútzenberger" becomes "Schütze
opher Hanusa 2009	P. 101. Equation (5) is missing a ')' after $f(\gamma)$ . The as " $\beta \star \gamma = \{ (e(\beta, f(\gamma)))$ ".
	P. 118, title of Note II.11: "the Ehrenfest <sup>2</sup> model", to what several readers think. It is an intended type was done jointly by Paul and Tatiana Ehrenfest, hu
afni	P. 123, Figure II.8. The estimate for "all cycles $\leq r$

Ayla Gafni 24/07/2009

Ayla Gafni 24/07/2009

Manuel Kauers 16/09/2009 Christopher Hanusa 12/08/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

P. 67, line -9. Insert a long space (\qquad) after the symbol " $\Longrightarrow$ ".
P. 77, Eq. (80). The figure could be cleaned.
P. 81, three lines below Equation (85). The equation for $\mathcal{H}$ should be " $\mathcal{H} = \mathcal{Z} + \mathcal{Z} \times \mathcal{H} + \mathcal{Z} \times \mathcal{H} \times \mathcal{H}$ ".
P. 86, Note I.60; line +2, read as "view $\mathcal{A}$ "; second display, read as "USEQ( $\mathcal{B}$ ). [I.e., change italics to calligraphic.]
P. 89, proof of Theorem I.5, last displayed equation. Delete the extra space between $d$ and the vertical bar in " $d \mid n$ ".
P. 95, footnote. "Schútzenberger" becomes "Schützenberger".
P. 101. Equation (5) is missing a ')' after $f(\gamma)$ . That is, the equation should start as " $\beta \star \gamma = \{ (e(\beta, f(\gamma)))".$
P. 118, title of Note II.11: "the Ehrenfest <sup>2</sup> model". This is not a typo, contrary to what several readers think. It is an intended typographical pun, since the work was done jointly by Paul and Tatiana Ehrenfest, husband and wife.
P. 123, Figure II.8. The estimate for "all cycles $\leq r$ " should read $\approx n^{n(1-1/r)}$ .
P. 123, last paragraph, line -3: "permutation" becomes "permutations".
P. 124, line -13. Overfull hbox at the end of the line.
P. 125, line -2. Last sentence should begin "Variations of these constructions"
P. 139, line -1. Read: " $\partial_z A(z)$ " [instead of $A(z)$ ].
P. 142, line 12. In case (i), " $\{\epsilon\}$ " becomes " $\{\epsilon\}$ ".
P. 145, line -12. Read as "Since the root of $\underline{a}$ tree".
P. 158, Equation (10). Replace $E$ by $\mathbb{E}$ .

clearer to read as "the characteristc <u>function</u> is".

P. 158, line -11. Read the reference as "[205, Ch. X]". (i.e., add period.)

P. 161, Section III.2.2, line +4. Delete comma after "one has" at the end of the line.

 $\mathbf{2}$ 

Manue 16/09/

Manue 16/09/

Manue 16/09/

 $\frac{\text{Christo}}{12/08}$ 

Robin 30/07/

 $\frac{Christo}{12/08}$ 

Manue 16/09/

Christo 12/08/

Ayla Gafni 24/07/2009

Manuel Kauers 16/09/2009

Ayla Gafni 24/07/2009

P. 167, line -3. Read as "(e.g., "). (I.e., insert comma and space after "e.g.".)	Manuel Kauers 16/09/2009
P. 169, line-14. Delete the stray comma in the first of the two compositions.	Robin Chapman 30/07/2009
P. 178, Prop III.6: comma missing between SET and Cyc. Thus, read as "where $\mathfrak K$ is one of SEQ, SET, Cyc."	Christopher Hanusa 12/08/2009
P. 186, first displayed equation. In the formula, " $\cdots u_r a_r$ " becomes " $\cdots + u_r a_r$ ".	Manuel Kauers 16/09/2009
P. 187, line 2 (displayed equation). Change " $n_r$ " to " $n_r$ !".	Manuel Kauers 16/09/2009
P. 188, Note III.24, first display. The last given term should be $f'(g(z))g''(z)$ (but not $f'(z)g''(z)$ ).	Christopher Hanusa 12/08/2009
P. 188, line-2, regarding Faà di Bruno: "canonized" becomes "beatified". Note: the MacTutor site (wrongly?) implies canonization. The Wikipedia notice is taken (so far?) as the authoritative source.	Robin Chapman 30/07/2009
P. 189, Example III.16. Line 4 should refer to Figure II.15 of Chapter II (but <i>not</i> to Figure III.15)	Christopher Hanusa 12/08/2009
P. 200, line-11. Read as $a(u) = zu + zuF(z, 1)/(1 - zu)$ (instead of $a(u) = zu + F(z, 1)/(1 - zu)$ ).	Christopher Hanusa 12/08/2009
P. 206, two lines after Note III.36. There is perhaps a spurious space before "intensely".	Manuel Kauers 16/09/2009
P. 206, last line. Read "inclusion–exclusion" (missing en-dash).	Christopher Hanusa 12/08/2009
P. 207, line 8. Change two occurrences of " $E$ " to " $\mathcal{E}$ ".	
P. 214, Note III.40, line 4. Read as "marked by $u$ . Setting $u \mapsto w - 1$ in $V$ then gives $B(z, w)$ as". Equation (78): replace $u$ by $w$ throughout.	
P. 230, line 2. There is perhaps a spurious space before "over".	Manuel Kauers
	16/09/2009 Manuel Kauers
P. 233, line -8. Consider changing " $\gamma$ is one-to-one" to " $\gamma$ is one-to-one (injective)", as the term "injective" is used in other parts of the book.	16/09/2009
P. 238, line +7. Overfull blox: consider changing the beginning of the line to "" for an elementary function $E(z)$ ".	Manuel Kauers 16/09/2009
P. 241. Consider increasing the size of fonts for axis labels.	Manuel Kauers 16/09/2009
	Manuel Kauers 16/09/2009

P. 243, Section IV.3.2, line +6. Read as  $|a_n| >_{i.o.} (K - \epsilon)^n$ . I.e., change "i.o" to "i.o.".

P. 246. Inequality at the bottom, line-2:  $\frac{f_{n+1}}{r^{n+1}}$  becomes  $f_{n+1}r$ .

P. 249, line +9. Read as "for all combinatorial classes associated with iterative specifications".

P. 249, 3 and 4 lines after the diagram relative to  $g \circ f$ : Consider relacing "Id" by "Id. (Check for consistency in other parts of the book.)

P. 252, footnote 7: "explicit" becomes "explicit".

P. 254–255, Example IV.4. Consider replacing "Tr" and Wa by "Tr" and "Wa".

P. 256, Note IV.26. In the displayed equation, insert a  $(-1)^r$  factor after "C =".

P. 262, line -1: "p. 349)" becomes "p. 349.)".

P. 264, paragraph "Pure periodicities", line +8: "or order" becomes "of order".

P. 265, line -9, first sentence of last paragraph before I.32: "some open problem" becomes "some open problems".

P. 269, Note IV.36. Replace "S(r)" by  $S_r$ .

P. 281, line -8. Overfull hbox.

P 285, beginning of second paragraph. Read as "the quotient of two functions".

P. 286, line -16, third sentence of last paragraph before bibliographic notes: "appreciably more complicated that poles" becomes "appreciably more complicated than poles".

P. 294, line -12. Add comma: "a neighbourhood of  $\sigma$ ,".

P. 296, line +4 of Example V.1. Read as "and belong to the unlabelled universe  $(\mathcal{C})$  or to ...". (I.e., replace the *first* occurrence of "labelled" on that line by "<u>un</u>labelled".

P. 298, line -16. It's preferable to read as "corresponding to  $S(z) = z^2 + z^3 + z^5 + \cdots$ ,". (Indeed, S(z) is defined on the previous page, whereas G(z) is from the more general discussion on p. 294.)

P. 302, line +2 of Proof. Read as "any dominant pole  $\alpha$ ". (I.e., delete comma.)

P. 303, end of long paragraph, middle of page. Insert period after "and so on".

Ayla Gafni 24/07/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Ayla Gafni24/07/2009

Manuel Kauers 16/09/2009

Miklos Bóna05/12/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Ayla Gafni 24/07/2009

Christopher Hanusa 12/08/2009 Manuel Kauers 16/09/2009

Christopher Hanusa 12/08/2009

Ayla Gafni 24/07/2009

Manuel Kauers 16/09/2009

Clemens Heuberger 17/12/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

24/07/2009 Christopher Hanusa 12/08/2009 Ayla Gafni 24/07/2009 Ayla Gafni 24/07/2009

Ayla Gafni

P. 311. First displayed equation should read "  $\Phi^*(s) = -\frac{\Gamma(s)}{1-2^s}$ ". (I.e., insert a Ayla Gafni 24/07/2009 minus sign before righthand side.)

P. 315, Note V.12. In the first display, write  $\Phi(w) \equiv \Phi(w; \xi, q)$  [i.e., change comma to semicolon, so as to be in agreement with the second display.

P. 308, footnote 3. Delete spurious comma and replace by a closing parenthesis:

P. 310, line -3, last displayed equation: error term should be  $O\left(\frac{\log^2 n}{\sqrt{n}}\right)$ .

P. 318, Note VI.13. "To each pairs" becomes "To each pair".

" $\{\pi\} = 0.14159\cdots$ ," becomes " $\{\pi\} = 0.14159\cdots$ )."

P. 310, Equation (27):  $e^{-2y}$  becomes  $e^{-y \log 2}$ .

P. 318, Section V.4, line +3. Beginning of line becomes "and Motzkin paths".

P. 322, proof of Proposition V.3, display. " $\mathcal{H}_{00}$ " should be " $\mathcal{H}_{0,0}$ " (insert comma; 3 occurrences)

P. 322, line -9: overfull hbox ("namely").

P. 323, line -4. Mismatched parentheses; read:  $\mathcal{L}[z^j Q_l]$ .

P. 324, Theorem V.5: overfull hbox ("weighted").

P. 343 third line of proof: space missing between "parts" and "(i)-(v)".

P. 354, line-12. Read: "each edge exactly once".

P. 366, three lines after the figure: "spirit of this book," becomes "spirit of this book.".

P. 365, line -11. Add a comma after "Temperley [574, p. 66]".

P. 366, third displayed equation. The middle quantity  $k(uz)^k + (k+1)(uz)^{k+1} + \cdots$ should be changed to  $k(uz) + (k+1)(uz)^2 + \cdots$ . The equation becomes

$$\mathcal{L}[u^k] = k(uz) + (k+1)(uz)^2 + \dots = (k-1)\frac{uz}{1-uz} + \frac{uz}{(1-uz)^2}.$$

(The end result is correctly stated.)

P. 368, line. Add a comma before "with" in "and with 3 of these".

P. 370, line -13. "The initial state (is" becomes "The initial state is".

P. 371, line -2. EIS A000027.

Manuel Kauers 16/09/2009

Christopher Hanusa 12/08/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Christopher Hanusa 12/08/2009

Svante Janson 10/11/2008 Manuel Kauers 16/09/2009

Gadi Aleksandrowicz

22/09/2009

Manuel Kauers 16/09/2009

5

Manuel Kauers 16/09/2009

Clemens Heuberger 30/03/2009 Christopher Hanusa 12/08/2009 Christopher Hanusa 12/08/2009

Nick Beaton 21/09/2009 Manuel Kauers 16/09/2009

Ayla Gafni 24/07/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Ayla Gafni24/07/2009

Christopher Hanusa 12/08/2009

Manuel Kauers 16/09/2009

Steve Finch Jon Borwein 08/10/2009 P. 375, line -5. "have have" becomes "have".

P. 381, Theorem VI.1, second display. Replace  $n^{a-1}$  by  $n^{\alpha-1}$ .

P 383, Equation (20). In the figure, the bold **0** should be a bold **1**.

P. 384, displays of Note V.1 and Note V.4. Parentheses should be made bigger in  $O\left(\frac{1}{n}\right)$  and in  $O\left(\frac{1}{n^2}\right)$ , respectively.

P. 384, Note VI.3. There is a missing alternation of sign in the displayed formula: replace  $\lambda_{k,\ell}$  by  $(-1)^{\ell} \lambda_{k,\ell}$ .

P. 393, Theorem VI.4. "Let f(z) be function" becomes "Let f(z) be a function".

P. 394 Eqns (30), (31) and Fig. VI.7 step 2:  $z \to 1$  becomes  $z \to \zeta$ .

P. 394, Equation (31). Replace  $\sigma(z/\zeta)$ )" by " $\sigma(z/\zeta)$ ".

P. 398, lines -4 and -6. " $\tau_n^*$ " becomes " $\tau_n^*$ ".

P. 401, line 5, first sentence of VI.6: "its satisfies" becomes "it satisfies".

P. 402, (iii). Missing period after "itself SA".

P. 402, lines +16. Overfull hbox.

P. 403 , line -15. Read as "locally inverted,". (I.e., replace semicolon by comma in source file.)

P. 407, Note VI.17. Insert space after  $\psi(u^p)$ .

P. 409, lines +1. " $(1-)^r$  becomes " $(-1)^r$ ".

P. 412, Section V.2, line +11. Overfull hbox..

P. 412, Example V.10, second display. Align second occurrence of " $\Longrightarrow$ " with first ocurrence on previous line.

P. 425, line -8: "a product d independent" becomes "a product of d independent"

P. 426, lines -5, -6. The constant  $K \doteq 0.8825424006106063735858257$  admits a closed form, as first found by Steven Finch and proved by Jon Borwein (private communication, October 2009). The last line of the display giving K should mention this symbolic value

 $K = \frac{4\log 2}{\pi}.$ 

P. 432, Example VI.17. Delete spurious commas after  $v_1$  and  $v_2$  in " $\langle u_1, v_1 \rangle$ " and " $\langle u_2, v_2 \rangle$ ".

P. 443, line +11. Eliminate a spurious parenthesis at beginning of line: "p. 468))" becomes "p. 468)".

P. 450, line -6. Read as " $\mathbb{F}_p[X]$  to  $\mathbb{Z}[X]$ ". (I.e., replace parentheses by square brackets.)

P. 454, line -19: "one components" becomes "one component".

P. 460, line -10: beginning of line should read as "degree 1, n/8 of degree 2". (Correct spelling of "degree" and add comma after "1".)

P. 461, centred table below Eq. (34): uncapitalize "Binary".

P. 462, line -8: "number of <u>a</u> cyclic" becomes number of cyclic".

P. 462, line -1: "thanks to generating functions" (i.e., need a plural).

P. 469, Lemma VII.2, line 1: read as "be <u>a</u> generating function".

P. 473, Example VII.13. first display needs  $\mathcal{Z}$  instead of simple Z

P. 476, line -4: overfull hbox.

P. 478, first display below Figure VII.13. It's proven again: alcohol leads to fuzzy thinking. The stated OGF A(z) incorrect; it's shifted, so we have really given 1 + zA(z). The correct OGF starts as  $A(z) = 1 + z + z^2 + 2z^3 + 4z^4 + \cdots$ .

P. 478, last display: " $35z^9$ " becomes " $+35z^9$ .

P. 481, line -5. Read as " $\mathcal{I}^{\bullet\bullet} \cong MSET(\mathcal{H})$ ". Line -3, formula (59) is to be changed into  $\mathcal{I}^{\bullet} + \mathcal{I}^{\bullet\bullet} \cong \mathcal{I} + (\mathcal{H} \times \mathcal{H})$ .

P. 486. Replace "EIS: Axxx" by "EIS Axxx" (use macro \EIS in source file).

P. 492, line +3: read as " $\lambda(\rho) = 1$ . In effect". (I.e., period replaces comma.)

P. 495, line -7. Possibly spurious space before "The quantity".

P. 496, line -7: " $y_1(z)$  becomes " $y_1(z)$ ".

Manuel Kauers 16/09/2009

Christopher Hanusa 12/08/2009

Manuel Kauers 16/09/2009

Jean-Philippe Conard 9/04/09 Svante Janson 29/05/2009

Manuel Kauers 16/09/2009

Nicolas Broutinxx/05/2009

Manuel Kauers 16/09/2009

 $\begin{array}{c} \text{Manuel Kauers} \\ 16/09/2009 \end{array}$ 

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009 8

P. 498, line +2: read as " $\sum_{n=1}^{\infty} c_n \omega^{jn} z^{n/k}$ ". (I.e., the exponent of  $\omega$  should be corrected.)

P. 502, line -6. Delete extra space between "EIS" and "A054727.

P. 503, line -7: "+  $+ 64z^{6}$ " becomes "+ $64z^{6}$ ".

- P. 510, Eq. (94). The equation should start as "0 = 1 z".
- P. 510, two lines before Proposition VII.9. "pull the BGF" becomes "pull out the BGF".

P. 511, line +6 of Example VII.21. change 'Polish" to "Polish". (I.e., single quote becomes a double quote.)

P. 513, line +7. Read: "principal" branch.

P. 519, Equation (112): " $c_r Y(z)$ " becomes  $c_r(z)Y(z)$ ".

P. 523, caption to Figure VII.21. Since we tried to write the book in English, rather than American, "center" should become "centre".

P. 524, Equation (123): " $\frac{du}{1-u}$ " becomes " $\frac{du}{1-u}$ ".

P. 525, one line before Propositio VII.12: "Summarizing ," becomes "Summarizing,".

P. 526, Note VII.21, line 9: check for the style of the closing parenthesis in "satisfies  $({\cal E})$  ".

P. 528, three lines before Proposition VII.13: delete spurious comma in "Singularity analysis,".

P. 543, line -17 (third paragraph): " $|f(z_0)(1-\lambda r)|$ " becomes " $|f(z_0)|(1-\lambda r)|$ ".

P. 548, line+13 (beginning of second paragraph after theorem VII.2): "does no fix" becomes "does not fix".

P. 553, TheoremVII.3, Item (ii): read as "a central approximation holds".

P. 560, line +8: "f'(r) = 0" becomes "f'(r) = 0,". (I.e., add comma.)

P. 562, line +4: "explicit rephrases," becomes "explicit, rephrases". (I.e., shift comma.)

P. 563, line +3 (first display). Erase the two symbols " $e \cdot$ " immediately following

Manuel Kauers 16/09/2009

Robin Chapman 30/07/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Ayla Gafni 24/07/2009

Ayla Gafni 24/07/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Miklos Bóna02/12/2009

the equal sign.

	Manuel Kauers
P. 563, Equation (44). Read as " $O\left(\exp\left(\sqrt{n}-n^{1/10}\right)\right)$ ". (I.e., change the style of the first opening parenthesis and add a matching closing parenthesis.)	16/09/2009
P. 564, line -5: read as "In terms of $G$ itself". (delete spurious comma.)	Manuel Kauers 16/09/2009
P. 568, Note VIII.11, line 2. Replace "fails to be <u>be</u> " by "fails to be".	Cyril Banderier 18/07/2009
P. 569, line -11: check overfull hbox (rephrase?).	Manuel Kauers 16/09/2009
P. 571, Note VIII.14. <i>EIS</i> <u>A0</u> 75729.	
P. 572, line -16: check overfull hbox (rephrase?).	Manuel Kauers 16/09/2009
P. 574, line -3: read as "a complete treatment.)". (I.e., interchange period and closing parenthesis.)	Manuel Kauers 16/09/2009
P. 579, line $+3$ : read as "Andrews'".	Manuel Kauers 16/09/2009
P. 584, line 7. EIS A000985 (delete one extra "A" in sequence reference).	
P. 598, two lines before Example VIII.14: check overfull hbox (rephrase?).	Manuel Kauers 16/09/2009
P. 598, line -6: delete extra space in "hashing algorithms by means".	Manuel Kauers 16/09/2009
P. 603, Note VIII.48: check overfull hbox (rephrase?).	Manuel Kauers 16/09/2009
P. 603, line -12: delete spurious space at the beginning of line, before "For".	Manuel Kauers 16/09/2009
P. 604, first line after figure caption: read as " $dz = (1 - t)e^{-t} dt$ ". (I.e., add $dt$ at the end of first formula.)	Manuel Kauers 16/09/2009
P. 619, line+13. This line, starting "The probability generating function", should end with "2 <sup>n</sup> " (but not with "2 <sup>-n</sup> ").	Christopher Hanus 12/08/2009
P. 621, Figure IX.5, line +4. Replace $e^{\lambda(1-u)}$ by $e^{\lambda(u-1)}$ , as the correct PGF of a Poisson( $\lambda$ ) random variable.	Clemens Heuberges 18/11/2009
P. 621, line +4 after figure caption. Read as "notion of convergence".	Manuel Kauers 16/09/2009
P. 627, Theorem IX.13, first line of statement. Replace " $E$ " by " $\mathbb{E}$ ". (I.e., use the usual symbol for Expectations.)	Clemens Heuberges 09/12/2009
P. 628, lines 13 and 14 of Example IX.5. Read as: "Choosing now the value $r = \log n$ in the statement of Theorem IX.3 provides". (I.e., delete "value" before "provides"	

9

usa

ger

ger

in the statement of Theorem IX.3 provides". (I.e., delete "value" before "provides" and insert "the value" after "now".)

10

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009 Manuel Kauers 16/09/2009

Clemens Heuberger 09/12/2009

Clemens Heuberger 17/12/2009

Clemens Heuberger 17/12/2009

Clemens Heuberger 17/12/2009

Manuel Kauers 16/09/2009

Cvril Banderier 25/06/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Cyril Banderier 18/07/2009

P. 632, Example IX.6, line +16. End sentence by a period.

P. 632, Example IX.6, line -3: "univaraite" becomes "univariate".

P. 633, Proof of Proposition IX.3. Replace "with q, one of the" by "with q one of the".

- P. 637, 3rd displayed equation from top: replace  $\frac{1}{(2-u)}$  by  $\frac{1}{(2-u)}$ .
- P. 642, 2nd line after Note IX. 18: "zentralle" becomes "zentrale".

P. 645, 3rd line after the proof of Proposition IX.5: read as "leads, after normalization".

P. 646, line -6, displayed equation. Replace " $\frac{1}{k!}$ " by " $\frac{1}{r!}$ " at the very beginning.

P. 650, line -5, immediately before Proposition IX.6. As the relevant notations are quite far away, earlier definitions should best be recalled before the statement of Proposition IX.6. Thus, to the paragraph preceding the statement, append the sentence (or footnote if it helps page breaks): "In what follows, we make use of our earlier notations (e.g., p. 251 and p. 411); namely for a generating function fwith nonnegative coefficients, we let  $\rho_f$  represent its radius of convergence and set  $\tau_f := f(\rho_f)$ , with  $\tau_f \leq +\infty$ ."

P. 650, line -2, statement of Proposition IX.6. Replace "with a unique dominant singularity at  $\rho_g$ , which is a simple pole" by "with the exception of a simple pole at  $\rho_q$ ".

P. 651, lines 5, -4, at the line break. Replace " $h(z) = \rho$ " by  $h(z) = \rho_q$ ". (Improve the write-up?)

P. 652, Proposition IX.7, 2nd line: delete extra parenthesis in "SEQ $(u\mathcal{H})$ )".

P. 652, Proposition IX.7. Variance is  $\mathbb{V}(X_n) \sim n \frac{\rho h''(\rho) + h'(\rho) - \rho h'(\rho)^2}{\rho^2 h'(\rho)^3}$ . (The corresponding formula in Theorem V.1, p. 294, is correct

P. 653, line -4: delete spurious coma after "Equation (35)".

P. 666, Note IX.33, line +4: read as "to build a finite automaton".

P. 671, line +3. It may be preferable to indicate summation indices: " $\sum$ " becomes

"
$$\sum_{n,k}$$
"

P. 673, line -2. Replace "<u>a</u> algebraic function" by "an algebraic function".

P. 680, 2nd display. Read:  $\mathcal{T} = \mathcal{Z}u + \mathcal{Z} \star \operatorname{SET}_{\geq 1}(\mathcal{T})$ . (I.e., a  $\mathcal{Z}$  is missing before  $\operatorname{SET}_{>1}$ .)

P. 683, end of long paragraph after the proof of Proposition IX.17: terminate the sentence with a period.

P. 684, indented paragraph tagged "*Linear differential equations*", line +4. Add closing double quotes after "regular" and after "irregular".

P. 691, last line before Example IX.31: change comma to period at the end of the paragraph.

P. 696, lines -3 and -5. Replace the two occurrences of "Theorem IX.14" by "Theorem VIII.8".

P. 697, line +8: delete spurious coma before "of the function".

P. 697, lines 12 and 13. Revert the sign of the inequalities, and read : " $\rho(1) \leq |\rho(u)|$ " and " $\rho(1) < |\rho(u)|$ ".

P. 697, line -4: insert opening brace "{" before  $\rho_i$ } $_{i \in \mathbb{Z}}$ .

P. 697, end of Example IX.34: poor spacing before end-of-example marker (black square). Rephrase?

P. 697, line -2: replace period by comma before "the other ones".

P. 701, Equation (91). Delete spurious opening parenthesis before  $1 + O(\kappa_n^{-1})$ .

P. 708, footnote 18. It could be added that "The function S is related to functions considered by Mittag-Leffler, Wright, and others [Erdelyi81c, §18.1]." The corresponding bibliographic entry is:

[Erdely81c] Erdélyi, A. *Higher Transcendental Functions* (book), Volume 3, Krieger publishing Company, Malabar, Florida, 1981.

P. 712, Proposition IX.24, Case (*ii*). This case needs checking and adjustments. From e-mail message by MN and OG: "It seems to us that the claim in Proposition IX.24 (*ii*) is not accurate. We believe that in this case the distribution is not bimodal since cores of constant size have probability 0 as  $n \to \infty$ ."

P. 718, quotation from the Bible: delete extra parenthesis at the end of the English translation.

P. 734, display at line-6. Read:  $\mathcal{L}_{i,j}^{(r)} = \mathcal{L}_{i,j}^{(r-1)} + \mathcal{L}_{i,r}^{(r-1)} \operatorname{Seq} \{\mathcal{L}_{r,r}^{(r-1)}\} \mathcal{L}_{r,j}^{(r-1)}$ . (I.e., delete spurious "(S)" in the middle of the formula.)

P. 739, line-1. Read as "If P(x), Q(x)" (thus replace ff by If).

 $\begin{array}{c} \text{Manuel Kauers} \\ 16/09/2009 \end{array}$ 

Manuel Kauers 16/09/2009

Manuel Kauers 16/09/2009

Cyril Banderier & Pawel Hitczenko 18/07/2009 Manuel Kauers 16/09/2009

Francesco Mainardi31/07/2009

Marc Noy & Omer Giménez 07/10/2009

Manuel Kauers 16/09/2009

Robert Brignall 6/11/2008

Christopher Hanusa 12/08/2009 Jean-Philippe Conard 2/06/2010

Paul-Olivier Dehaye 7/9/2009

Francesco Mainardi 29/07/2009

Nicla Bernasconi 17/02/2010

P. 751, lines 1–2. Read as "the notation  $a^{\underline{n}}$  for representing the rising factorial  $a(a+1)\cdots(a+n-1).$ Equations (24) and (26): change accordingly  $(\cdot)_n$  to  $(\cdot)^n$ . (Also check consistency of this notation.)

P. 759, Note B.22. The coefficient in the  $O(n^{-1})$  error term needs adjustment. Also, the coefficients  $g_j$  need to be specified precisely.

P. 762, Note B.24. The last display should have  $S_n^r$  replaced by  $S_n^{(r)}$ , in accordance with earlier conventions in this Note.

P. 774. Equation (4). Middle line should read:

$$\mu^{(2)} = \left. \frac{d^2}{ds^2} \lambda(s) \right|_{s=0} = -\left. \frac{d^2}{dt^2} \phi(t) \right|_{t=0}$$
place  $\frac{d}{dt}$  by  $\frac{d^2}{dt^2}$ .)

P. 775, Figure C.1, line +5. Replace  $\frac{\lambda^k}{k!}$  by  $\frac{\lambda^k}{k}$ , to get the correct form of the probabilities of a logarithmic-series random variable. (The form given on p. 297 is correct.)

P. 775, Figure C.1, line +6. Replace  $e^{\lambda(1-u)}$  by  $e^{\lambda(u-1)}$ , as the correct PGF of a  $Poisson(\lambda)$  random variable.

Cyril Banderier 18/07/2009

Christopher Hanusa 12/08/2009

(I.e., re]dt  $dt^2$   $dt^2$ 

P. 785, Ref. [178]. Replace "Ruble" by "Rubel".

References

P. 792, references [377-379]. It would be desirable to have TAOCP vol 2 come before TAOCP vol 3 in the bibliography (hack bibtex?).